## Practice Paper 2

Please write clearly in block capitals.

Centre number


Candidate number


Surname
Forename(s)
Candidate signature

## GCSE

Mathematics
Higher


## Summer 2018

Time allowed: 1 hour 30 minutes

## Materials

For this paper you must have:

- a calculator
- mathematical instruments.



## Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.


## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80 .
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to the answer book.


## Advice

| For Examiner's Use |  |
| :---: | :---: |
| Pages | Mark |
| 3 |  |
| $4-5$ |  |
| $6-7$ |  |
| $8-9$ |  |
| $10-11$ |  |
| $12-13$ |  |
| $14-15$ |  |
| $16-17$ |  |
| $18-19$ |  |
| $20-21$ |  |
| $22-23$ |  |
| TOTAL |  |

- In all calculations, show clearly how you work out your answer.

Practice Paper Overview

| Q | Topic | Mark | Total |
| :---: | :---: | :---: | :---: |
| 1 | Algebraic Multiples |  | 1 |
| 2 | Algebraic Factors |  | 1 |
| 3 | Scalar and Resultant Vectors |  | 1 |
| 4 | Congruence |  | 2 |
| 5 | Frequency Tree |  | 4 |
| 6 | Dimensional Analysis |  | 3 |
| 7 | Reverse Percentage and Percentage Increase |  | 3 |
| 8 | Error Interval - Truncation |  | 2 |
| 9 | Scatter Graph |  | 3 |
| 10 | Construction |  | 2 |
| 11 | Expanding Brackets |  | 3 |
| 12 | Percentage Problem |  | 3 |
| 13 | Angles in Polygons Problem |  | 3 |
| 14 | Product of Prime Factors |  | 2 |
| 15 | Right Angled Trigonometry |  | 2 |
| 16 | Quadratic Sequence |  | 3 |
| 17 | Proportion |  | 3 |
| 18 | Area of a sector problem |  | 5 |
| 19 | Perpendicular Lines |  | 1 |
| 20 | Product Rule for Counting |  | 1 |
| 21 | Identities |  | 3 |
| 22 | 3D Pythagoras |  | 3 |
| 23 | Combined Transformation |  | 3 |
| 24 | Circle Theorem Proof |  | 3 |
| 25 | Mean from a Table |  | 3 |
| 26 | Percentage Change |  | 4 |
| 27 | Area Underneath a Curve |  | 4 |
| 28 | Functions |  | 6 |
| 29 | Similarity |  | 3 |
|  | Total |  | 80 |

1 Circle the lowest common multiple (LCM) of $6 x^{2} y$ and $12 x^{4} y^{3}$ $2 x y$ $3 x^{2} y$ $6 x y$
$12 x^{4} y^{3}$
$12 x^{6} y^{4}$
$24 x^{4} y^{3}$

2 Circle the highest common factor (HCF) of $6 x y^{2}$ and $12 x^{4} y$
$2 x y \quad 3 x^{2} y \quad 6 x y \quad 12 x^{4} y^{3} \quad 12 x^{6} y^{4} \quad 24 x^{4} y^{3}$

3

$$
\boldsymbol{a}=\binom{3}{-2} \text { and } \boldsymbol{b}=\binom{-2}{5}
$$

Circle the vector $2 \boldsymbol{a}+\mathbf{b}$.
$\binom{2}{3}$
$\binom{4}{9}$
$\binom{8}{1}$
$\binom{4}{1}$
$\binom{4}{-9}$

4 Here are four triangles


Not drawn
accurately
B


D


4 (a) Which two triangles are congruent? Circle your answers.
A
B
C
D

4 (b) Circle the reason for your answer to part (a).
SSS
ASA
SAS
RHS
RHS

5200 adults are surveyed at random in at a bingo hall.
$32 \%$ of the customers are male.
106 out of the 200 adults have never won.
The females claimed to have won and lost in the ratio of 3:5.

5 (a) Complete the frequency tree.


5 (b) A person is selected at random.
Given that the person selected is male.
Calculate the probability that he will win.
$\qquad$
$\qquad$

Answer $\qquad$

6 There are three novelty golf balls in a cuboid shaped box.
Each golf ball has a diameter of 4.2 cm
accurately

Calculate the volume of the box.
Give your answer correct to 1 decimal place.

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

7 Joe sells caricature portraits.
He currently adds $28 \%$ profit to the cost price.
He sells the portraits for $£ 256$ each.
He wants to increase the profit to $35 \%$ of the cost price.
How much should he sell each picture for?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Answer

8 Komal truncates a number, $x$, to one decimal place.
The result is 9.2
Write down the error interval for $x$.
[2 marks]
$\qquad$
$\qquad$
$\qquad$

$$
\leq x<
$$



9 (a) Describe the relationship between the air temperature and the height above sea level.
$\qquad$
$\qquad$
$\qquad$

9 (b) Find an estimate of the height above sea level when the air temperature is $-1.5^{\circ} \mathrm{C}$.
[2 marks]
$\qquad$
$\qquad$
$\qquad$

Answer

10 Use the ruler and compasses to construct the perpendicular to the line segment $A B$ that passes through the point $P$.
You must show all construction lines.


11 Show that

$$
(2 x-1)(x+3)(x-5)=2 x^{3}-5 x^{2}-28 x+15
$$

for all values of $x$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

12 In a school, 70\% of the students are male.
$30 \%$ of the girls don't get school dinners.
$20 \%$ of the boys don't get school dinners.
What percentage of the students get school dinners?
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

13 The diagram shows two regular pentagons and a square.


Work out the size of the angle marked $x$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

14 Express 315 as a product of its prime factors in index form.
[2 marks]

## Answer

15 Calculate the size of the angle marked $x$.

6.2 cm
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer cm

16 Here is a quadratic sequence.

$$
5
$$

14
27 44

The expression for the nth term of this sequence is $p n^{2}+q n$.
Find the value of $p$ and the value of $q$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$$
p=
$$

$\qquad$

$$
q=
$$

$\qquad$

17 (a) It takes 3 men 12 hours to build a shed.
How long would it take 4 men to build the shed?

## Answer

17(b) Comment on an assumption you made in part (a) and the impact this could have on the length of time taken to build the shed.
$\qquad$
$\qquad$
$\qquad$

18 A path is placed around a circular section of grass on the edge of a lakes dock.

Grass


Andrea wants to cover the path with gravel.
Each bag of gravel covers $5 \mathrm{~m}^{2}$ and costs $£ 3.99$.
How much will it cost to cover the path in gravel?
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

19 Circle the equation of a line that is perpendicular to $y=2 x-5$

$$
\begin{gathered}
y=5 x-2 \quad y=\frac{1}{2} x-5 \quad y=2 x+6 \\
y=-2 x+5 \quad y=5-\frac{1}{2} x
\end{gathered}
$$

20 A menu has a choice of 4 starters, 3 mains and 2 desserts. How many different choices of 3 course meals are there?

Circle your answer.

9
12
14
24
48
96

21 Find the solution for $a$ and $b$ by equating the coefficients.

$$
x^{2}+12 x+9 \equiv(x+a)^{2}+b
$$

$$
a=
$$

$b=$ $\qquad$

22 The diagram represents a cuboid ABCDEFGH..


Not drawn accurately

Find the length of AG.
Give your answer correct to 3 significant figures.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

23


Triangle $\mathbf{A}$ is drawn on a coordinate grid.
The triangle $\mathbf{A}$ is reflected in the line $x=2$ and
then reflected in the line $y=-1$ to give triangle $\mathbf{B}$.
Describe fully the single transformation which maps triangle $\mathbf{A}$ onto triangle $\mathbf{B}$.
[3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$


Not drawn accurately
$A, B$ and $C$ are points on the circumference of a circle, centre $O$.
Prove that angle $A O C$ is twice the size of angle $A B C$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

25 The heights of 60 trees in New Forest were recorded in the table below.

| Height <br> $\mathbf{( h , ~ c m ) ~}$ | Number of trees |
| :---: | :---: |
| $h<2$ | 0 |
| $2 \leq h<4$ | 13 |
| $4 \leq h<8$ | 17 |
| $8 \leq h<16$ | 21 |
| $16 \leq h<20$ | 9 |

Calculate an estimate for the mean height of the trees.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

26 Jake sells fish.
In March, he sold 800 fish.
In April, Jake said he sold $30 \%$ more fish than in march.
In May, Jake said he sold 10\% fewer fish than in April.
Jake claims his sales have increased by $20 \%$ in total since March.
Comment on Jakes Claim.
[4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

27 Here is a velocity-time graph for a bike journey.


27 (a) Work out an estimate for the total distance travelled in the first 60 seconds.
$\qquad$
$\qquad$
$\qquad$

## Answer

$\qquad$
27 (b) Is your answer to (a) an underestimate or an overestimate of the actual distance?
Give a reason for your answer.
$\square$ Underestimate $\square$ Overestimate
$\square$

28 For all values of $x$,

$$
\begin{gathered}
f(x)=4-x \\
g(x)=x^{2}-2
\end{gathered}
$$

28 (a) Find $g^{-1}(x)$
[2 marks]

## Answer

28 (b) Solve the equation

$$
g f(x)=26
$$

[4 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

29 There are two similar boxes.


Not drawn

Box A has a volume of $200 \mathrm{~cm}^{3}$
Box $B$ has sides double the length of Box $A$.
What is the volume of Box $B$ ?

Answer

There are no questions printed on this page

DO NOT WRITE ON THIS PAGE ANSWER IN THE SPACES PROVIDED

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